

# APPLICATION OF A SOIL CAP MODEL TO GROUND MOTION ANALYSES

University of New Mexico Albuquerque, NM 87131

February 1978

**Final Report** 



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JOSEPH H. AMEND, III

auch H amed II

Captain, USAF Project Officer

STEWART W. JOHNSON.

Lt Colonel, USAF

Chief, Technology Applications Branch

FOR THE COMMANDER

FRANK J. LEECH.

Lt Colonel, USAF

Chief, Civil Engineering Research Division

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A soil cap model was analyzed and an equation-of-stadeveloped and implemented in a one-dimensional, wave was used to match laboratory data of a sand material in-oitu properties of a clay material from Cylindric Comparisons were made between the experimental data the cap model and another constitutive model; both m with the cap model providing slightly better agreeme	-propagation code. The mod and to estimate the dynami al <i>In-Situ</i> Test (CIST) data and the results obtained wi odels gave similar results
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### PREFACE

This report represents the culmination of work performed by many individuals. The author wishes to acknowledge the support of Dr. Howard L. Schreyer, formerly of the Civil Engineering Research Facility (CERF), who initiated this work. A substantial portion of this report is based on Dr. Schreyer's research.

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# SECTION I

Over the past several years, there has been considerable effort devoted to the development of mathematical models to represent the nonlinear, inelastic behavior of geologic materials. These models are necessary for the accurate analysis and prediction of ground motion response and structure/medium interaction under explosive, earthquake, and vibration excitation. Several material models are currently in use; e.g., variable moduli models and various elastic/plastic models (ref. 1).

The objectives of this effort were to investigate a particular capped, elastic/plastic material model and to implement this model into a wave-propagation code for use in ground motion calculations. Weidlinger Associates have made significant advancements in the development of cap models (re?s. 2, 3). The work reported here, much of which is based on their research, was undertaken to complement earlier work (ref. 2) by providing a fairly detailed analysis of one specific form of the general soil cap model.

The general soil cap model is an elastic, nonideally plastic model with yield criteria that combine both ideal plasticity and strain hardening. This model has been used to simulate the uniaxial strain, standard triaxial stress, and proportional loading tests performed in laboratory experiments (ref. 1) and also satisfies theoretical requirements for uniqueness and stability. A brief summary of the general soil cap model and a similar model for rock is contained in reference 1.

<sup>1.</sup> Nelson, I., Baron, M. L., and Sandler, I., "Mathematical Models for Geological Materials for Wave-Propagation Studies," Shock Waves and the Mechanical Properties of Solids, Syracuse University Press, Syracuse, New York, 1971.

Sandler, I., and Rubin, D., A Modular Subroutine for the Cap Model, Report DNA-3875F, Defense Nuclear Agency, Washington, D.C., January 1976.

Sandler, I. S., DiMaggio, F. L., and Baladi, G. Y., "Generalized Cap Model for Geologic Materials," Journal of the Geotechnical Engineering Division, ASCE, Vol. 102, No. GT7, July 1976, pp. 683-699.

Subsequent sections of this report describe the total strain increment procedure utilized in the general soil cap model. A computer code was written to evaluate the material constants for a prescribed total strain path, and a computer subroutine based on the total strain increment procedure was implemented in a one-dimensional wave-propagation code. Comparisons of responses calculated with the specified cap model and another constitutive model were made for several materials subjected to shock loadings. Finally, the limitations and problems associated with the cap model were addressed and recommendations for future use were developed.

### SECTION II SOIL CAP MODEL

#### TOTAL STRAIN INCREMENT PROCEDURE

To analyze any plasticity model, it is beneficial to develop a method for evaluating the material behavior for a prescribed stress or strain path. Since many wave-propagation codes utilize the total strain increment procedure, this method was used to study the soil cap model. The following derivations are based on the assumption that the total strain increments are known. However, before the total strain increment approach is described, some background information must be presented.

In classical plasticity theory, the components of the plastic strain rate tensor can be expressed as

$$de_{ij}^{p} = d\lambda \frac{\partial \psi}{\partial \sigma_{ij}}$$
 (1)

where

 $de_{ij}^{p}$  = plastic strain rate or increment  $d\lambda$  = scalar function

 $\psi$  = plastic potential function

 $\sigma_{ii}$  = stress components

If the plastic potential function is assumed to be identical to the yield function, f, an associated flow rule is obtained; i.e.,

$$de_{ij}^{p} = d\lambda \frac{\partial f}{\partial \sigma_{ij}}$$
 (2)

The following expressions describe the usual plasticity relationships for infinitesimal strains:

$$d\sigma_{ij} = C_{ijk\ell} de_{k\ell}^{e}$$

$$= C_{ijk\ell} de_{k\ell} - de_{k\ell}^{p}$$
(3)

where

Cijkl = compliance components

 $de_{b\ell}^{e}$  = elastic strain rate or increment

 $de_{bP}$  = total strain rate or increment

The consistency equation for the yield function can be expressed as

$$\frac{\partial f}{\partial \sigma_{ij}} d\sigma_{ij} + \frac{\partial f}{\partial e_{ij}^{p}} de_{ij}^{p} = 0$$
 (4)

where f is assumed to be a function of stress and plastic strain. Combining equations (2), (3), and (4) results in the following expressions:

$$- d\lambda \left(\frac{\partial f}{\partial e_{i,j}^{p}}\right) \left(\frac{\partial f}{\partial \sigma_{i,j}}\right) = C_{i,j,k,\ell} \left(de_{k,\ell}\right) - d\lambda \left(\frac{\partial f}{\partial \sigma_{k,\ell}}\right) \left(\frac{\partial f}{\partial \sigma_{i,j}}\right)$$
(5)

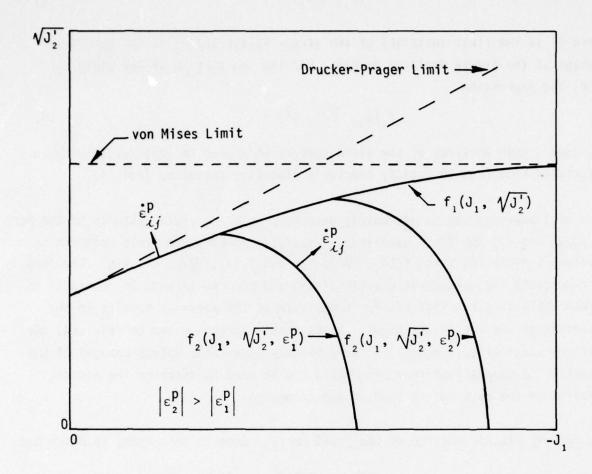
or

$$d\lambda = \frac{C_{ijk\ell} de_{k\ell} \left(\frac{\partial f}{\partial \sigma_{ij}}\right)}{C_{ijk\ell} \left(\frac{\partial f}{\partial \sigma_{k\ell}}\right) \left(\frac{\partial f}{\partial \sigma_{ij}}\right) - \left(\frac{\partial f}{\partial e_{ij}^p}\right) \left(\frac{\partial f}{\partial \sigma_{ij}}\right)}$$
(6)

In summary, if the total strain increments are known,  $d\lambda$  can be computed from equation (6). The plastic strain increments are then obtained from equation (2) and the elastic strain increments are determined by subtracting the plastic strain increments from the total strain increments. Finally, the stress increments are derived from equation (3).

#### YIELD CRITERIA

Figure 1 shows the general soil cap model yield surface in two-dimensional stress space. The elastic/plastic model is rate-independent and combines ideal plasticity and strain hardening. In its most general form, the yield criterion is a function of all the stress components and the stress/strain history of the material.



 $J_1$  = first invariant of stress tensor  $J_2^{i}$  = second invariant of stress deviator tensor  $\varepsilon_1^{p}$ ,  $\varepsilon_2^{p}$  = volumetric plastic strains  $\varepsilon_{ij}^{p}$  = components of plastic strain rate tensor

Figure 1. Yield Surface for General Soil Cap Model (ref.1)

For the particular cap model studied, the ideally plastic portion of the yield surface was assumed to be of the form

$$f_1(J_1, \sqrt{J_2^T}) = 1$$
 (7)

where  $J_1$  is the first invariant of the stress tensor and  $J_2^{'}$  is the second invariant of the stress deviator tensor. For the cap portion of the yield surface, the expression

$$f_2(J_1, \sqrt{J_2'}, \epsilon^p) = 1$$
 (8)

was used. Both portions of the yield surface were used in conjunction with an associated flow rule to satisfy Drucker's stability postulate (ref. 4).

Most soil behavior can be adequately described by using yield criteria in the form of equations (7) and (8). Weidlinger Associates specify the yield criteria in a slightly different form;  $f_1(J_1, \sqrt{J_2'}) = 0$  and  $f_2(J_1, \sqrt{J_2'}, \epsilon^p) = 0$ . The term  $\epsilon^p$  represents the volumetric plastic strain and the cap expands or contracts in stress space as a function of  $\epsilon^p$ . Compaction of the material results in the expansion of the cap to the right. Since strain hardening can be reversed, the soil cap model allows control of the dilatancy (inelastic volume change) of the material. A generalized form of Hooke's Law is used to describe the elastic behavior of the material in loading and unloading.

The ideally plastic portion of the yield surface used in this study is described by

 $f_1(J_1, \sqrt{J_2'}) = \sqrt{J_2'} / \left(\alpha - \gamma e^{\beta J_1}\right)$  (9)

where  $\alpha$ ,  $\gamma$ , and  $\beta$  are material constants. This exponential form of the yield surface is used to fit the data obtained from triaxial stress experiments.

Drucker, D. C., "On Uniqueness in the Theory of Plasticity," Quar. Appl. Math., 14, 1956, pp. 35-42.

It was assumed that the cap portion of the yield surface could be described by a family of ellipses; i.e.,

$$f_2(J_1, \sqrt{J_2'}, \epsilon^p) = \frac{1}{R^2b^2} \left[ R^2J_2' + (J_1 - C)^2 \right]$$
 (10)

where

$$Rb = C - X \tag{11}$$

and

R = ratio of major to minor axis of ellipse

 $X = J_1$  value at intersection of cap and  $J_1$ -axis

C = J, value at center of ellipse

 $b = \sqrt{J_2}$  value at  $J_1 = C$ 

These ellipses have horizontal tangents at their intersection with the ideal yield surface. This forces the plastic strain rate vector, which is always perpendicular to the yield surface, to be vertical at the intersection and, thus, precludes further cap motion and controls the amount of dilatancy.

The function X depends on the volumetric plastic strain and was assumed to be of the form

$$X\left(\varepsilon^{p}\right) = \left[\ell n \left(1 + \frac{\varepsilon^{p}}{W}\right)\right] / D + Z \tag{12}$$

for this study. Hydrostatic test data for a sand were used by DiMaggio and Sandler (ref. 5) to determine the specific form of equation (12), but other forms may be appropriate if they give a better representation of the hydrostatic behavior of the material. Additional constants that can be evaluated from various laboratory experiments are R, D, W, and Z. Details of the composite yield surface are shown in figure 2.

#### STRESS AND STRAIN GRADIENTS OF YIELD FUNCTIONS

It is necessary to compute the stress and strain gradients of the yield functions in a total strain increment procedure before equation (6) is applied. For the

DiMaggio, F. L., and Sandler, I. S., "Material Model for Granular Soils," Journal of the Engineering Mechanics Division, Proceedings of the American Society of Civil Engineers, Vol. 97, No. EM3, June 1971, pp. 935-949.

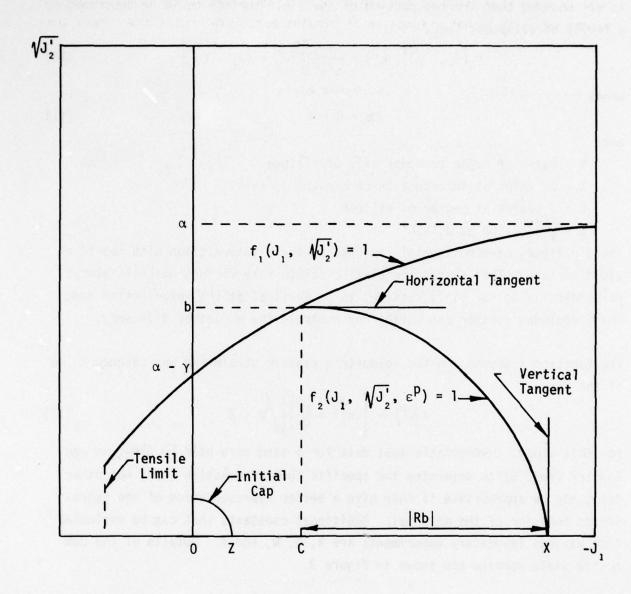


Figure 2. Composite Yield Surface for Specific Soil Cap Model

ideally plastic portion of the yield surface, only the stress gradient is required since  $\mathbf{f}_1$  is not a function of strain; but, both stress and strain gradients are needed for the cap portion of the yield surface.

The stress gradient of  $f_1$  can be expressed as

$$\frac{\partial f_{1}}{\partial \sigma_{ij}} = \frac{\frac{1}{2} \frac{\partial J_{2}^{'}}{\partial \sigma_{ij}^{'}}}{\sqrt{J_{2}^{'}} \left[\alpha - \gamma e^{\beta J_{1}}\right]} + \frac{\sqrt{J_{2}^{'}} \gamma \beta e^{\beta J_{1}} \frac{\partial J_{1}}{\partial \sigma_{ij}^{'}}}{\left[\alpha - \gamma e^{\beta J_{1}}\right]^{2}}$$

$$= \frac{f_{1}}{2J_{2}^{'}} \left[\sigma_{ij}^{d} + 2f_{1} \sqrt{J_{2}^{'}} \gamma \beta e^{\beta J_{1}} \delta_{ij}\right] \tag{13}$$

where  $\sigma_{ij}^{\mathbf{d}}$  are the components of the deviatoric stress tensor and  $\delta_{ij}$  is the Kronecker delta;  $\mathbf{f}_1$  is defined in equation (9). Similarly, the stress gradient of  $\mathbf{f}_2$  [equation (10)] is

$$\frac{\partial f_2}{\partial \sigma_{ij}} = \frac{1}{R^2 b^2} \left[ R^2 \sigma_{ij}^d + 2(J_1 - C) \delta_{ij} \right]$$
 (14)

Before an explicit form of the strain gradient of  $f_2$  can be obtained, some intermediate partial derivatives must be calculated. Since the function X [eq. (12)] depends solely on  $\epsilon^p$ , the strain gradient of X can be written as

$$\frac{\partial X}{\partial e_{ij}^{p}} = \frac{\delta_{ij}}{DW \left(1 + \frac{\varepsilon^{p}}{W}\right)}$$
 (15)

Equation (9) can be used to obtain the expression

$$b = \alpha - \gamma e^{\beta C}$$
 (16)

and hence

$$\frac{\partial b}{\partial e_{i,j}^{p}} = -\gamma \beta e^{\beta C} \left( \frac{\partial C}{\partial e_{i,j}^{p}} \right)$$

$$= \frac{1}{R} \left( \frac{\partial C}{\partial e_{i,j}^{p}} - \frac{\partial X}{\partial e_{i,j}^{p}} \right)$$
 (17)

where equation (11) has been used. Rearranging equations (16) and (17) gives

$$\frac{\partial C}{\partial e_{ij}^{p}} = \frac{\frac{\partial X}{\partial e_{ij}^{p}}}{\left(1 + R_{Y}\beta e^{\beta C}\right)}$$

$$= \frac{\delta_{ij}}{DW\left(1 + \frac{\epsilon^{p}}{W}\right)\left(1 + R_{Y}\beta e^{\beta C}\right)} \tag{18}$$

The strain gradient of b can then be written as

$$\frac{\partial \mathbf{b}}{\partial \mathbf{e}_{i,j}^{\mathbf{p}}} = \frac{-\gamma \beta \mathbf{e}^{\beta \mathbf{C}} \delta_{i,j}}{\mathsf{DW} \left( 1 + \frac{\varepsilon^{\mathbf{p}}}{\mathsf{W}} \right) \left( 1 + \mathsf{R} \gamma \beta \mathbf{e}^{\beta \mathbf{C}} \right)} \tag{19}$$

Combining equations (10), (12), (17), and (18) gives the expression for the strain gradient of  $f_2$  as

$$\frac{\partial f_{2}}{\partial e_{i,j}^{p}} = \frac{-2\left(\frac{\partial b}{\partial e_{i,j}^{p}}\right)}{R^{2}b^{3}}\left[R^{2}J_{2}^{i} + (J_{1} - C)^{2}\right] - \frac{2}{R^{2}b^{2}}(J_{1} - C)\frac{\partial C}{\partial e_{i,j}^{p}}$$

$$= \frac{-2\delta_{i,j}e^{-D(X - Z)}\left[f_{2}R^{2}b\beta(b - \alpha) + (J_{1} - C)\right]}{R^{2}b^{2}DW\left[1 + \beta(R\alpha + X - C)\right]} \tag{20}$$

The product of the strain and stress gradients is also required in equation (6) and this product is

$$\frac{\partial f_2}{\partial e_{i,j}^p} \frac{\partial f_2}{\partial \sigma_{i,j}} = \frac{-3\hat{c}e^{-D(X-Z)} \left[\hat{c} + 2f_2\beta \left(1 - \frac{\alpha}{b}\right)\right]}{DW \left[1 + \beta (R\alpha + X - C)\right]}$$
(21)

where

$$\hat{C} = \frac{2(J_1 - C)}{R^2 b^2}$$

#### **EVALUATION OF MATERIAL CONSTANTS**

Experimental data from triaxial stress experiments are required to evaluate the material constants which describe the yield function  $f_1$ . It is assumed

that a judicious choice of the constants  $\alpha$ ,  $\gamma$ , and  $\beta$  will define a yield surface which will adequately match the experimental yield data.

For large values of -J,, equation (9) becomes

$$f_1 \approx \frac{\sqrt{J_2'}}{\alpha}$$

and hence  $\alpha$ , which represents the von Mises Limit, can be determined if the  $\sqrt{J_2^{'}}$  values of the experimental data approach a constant as  $-J_1$  increases. If  $J_1 = 0$  the yield function  $f_1$  is

$$f_1 = \frac{\sqrt{J_2'}}{\alpha - \gamma}$$

The quantity  $(\alpha - \gamma)$  is proportional to the cohesion of the material, and  $\gamma$  can be determined once  $\alpha$  is chosen. The constant  $\beta$  controls the degree of curvature of the yield function  $f_1$ . Hence,  $\beta$  can be chosen to give the best approximation of the experimental data as  $\sqrt{J_2'}$  transitions from  $(\alpha - \gamma)$  to  $\alpha$ .

A hydrostatic test is required to evaluate the material constants which describe the cap portion of the yield surface. If a material is loaded hydrostatically, the stress field is defined by normal stress components that are all equal to the negative of the confining pressure, P, and shearing stress components that are identically zero. This hydrostatic behavior is represented in the cap model as

$$X = -3P$$

Equation (12) then becomes

$$-3P = Z + \frac{1}{D} \ln \left(1 - \frac{\mu^{D}}{W}\right)$$

or

$$\mu^{p} = W \left[ 1 - e^{-D(Z + 3P)} \right]$$

where  $\mu^{\textbf{p}}$  is the plastic volumetric compression. The total volumetric compression,  $\mu_{\textbf{r}}$  is then expressed as

$$\mu = \mu^{e} + \mu^{p}$$

$$= \frac{P}{K} + W \left[ 1 - e^{-D(Z + 3P)} \right]$$

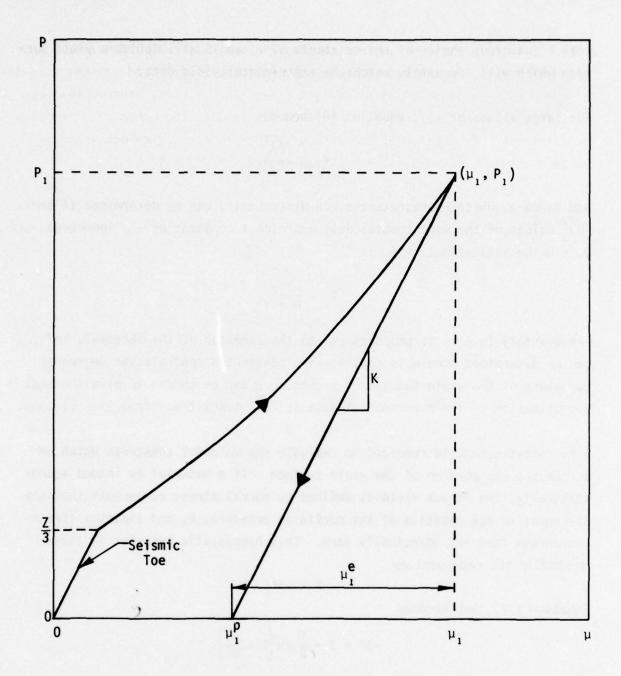


Figure 3. Assumed Hydrostatic Behavior in Loading and Unloading

where  $\mu^e$  is the elastic volumetric compression and K is the bulk modulus. The unloading portion of the hydrostat is assumed to be elastic and, hence, K is determined from the slope of this straight line (fig. 3). Any other unloading test, such as uniaxial strain, can be used to evaluate the other required elastic constants. Evaluation of the parameter Z is also required and its value can be estimated if a seismic toe exists in the hydrostat (fig. 3).

The parameters D and W determine the shape of the loading portion of the hydrostat. If it is desired to match the point on the hydrostat  $(\mu_1, P_1)$ , D and W must satisfy the relationship

$$\mu_1 = \frac{P_1}{K} + W \left[ 1 - e^{-D(Z + 3P_1)} \right]$$

Consequently, D and W can be varied until they produce a  $best\ fit$  of the loading portion of the hydrostat. Variations in D and W change the degree of concavity of the loading hydrostat. Hence, several plots of  $\mu$  versus P can be constructed for the various choices of D and W and a final engineering judgment can be made.

The final material constant (R) is determined by a trial-and-error process. An iterative procedure must be used to obtain the R value which gives results that are compatible with experimental data. Values of R in the range of 2.5 to 5 have been used and have produced satisfactory results.

# SECTION III COMPUTATIONAL PROCEDURES

The application of the cap model to wave-propagation problems was a two-fold process. Initially, a computer code which utilized the soil cap constitutive equations, Program ELLSTR (appendix A), was written so that the material constants could be evaluated for a prescribed total strain path. An equation-of-state subroutine based on the cap model (appendix B) was then implemented in a one-dimensional, wave-propagation code. Results were obtained from several material models subjected to simulated shock loadings and these data were compared with the results obtained from another constitutive model and actual experimental data.

Program ELLSTR computes stresses and elastic and plastic strain components for a prescribed total strain path. This program is based on the procedure outlined in section II for prescribed total strain increments. The total strain increment procedure for the soil cap constitutive model is described as follows.

The material constants and a parameter that controls the degree of subincrementation of the total strains are required as input to ELLSTR. The user also supplies sets of total strains, and the difference between two successive sets of total strains provides the strain increment set.

Initially, the incremental strains are assumed to be elastic and the stress components are computed on this assumption. Stresses are computed from the isotropic stress/strain relationship

$$\{\sigma\} = [C] \{e^e\}$$

where  $\{\sigma\}$  and  $\{e^e\}$  are the stress and elastic strain vectors, respectively, and [C] is the constitutive matrix. Once the stresses have been calculated the appropriate yield function,  $f_1$  or  $f_2$ , is evaluated. If the calculated value of  $J_1$  is greater than C,  $f_1$  is evaluated and if  $J_1$  is less than C,  $f_2$  is evaluated. If the value of the yield function is less than 1, the assumption of elastic behavior is presumed to be correct and the program reads in the next set of total strains. If the yield function is greater than 1, some

plastic deformations must occur to prevent f from exceeding 1. For this case, the total strains are reset to their previous values and the strain increments are then subdivided into a number of smaller increments. The number of subdivisions is proportional to the value of the computed yield function.

For any particular set of subincremental strains, the stresses and yield function are again evaluated, and if the resulting f is less than 1, the subincrement of strains is presumed to be elastic and the program proceeds with a new set of total strain subincrements. If the computed f exceeds 1, an iteration loop is entered in which new stresses and plastic strains are calculated based on equations (1) through (6). This loop terminates when f meets some criterion for satisfying the yield condition. The program uses a tolerance limit of  $0.99 \le f \le 1.01$  as the specified criterion.

There is a possibility that a value of f less than I can be calculated during the iteration loop and f can oscillate from a value greater than I to a value less than I. Significant errors can accumulate if the iteration loop terminates with a yield function value less than I. A method has been adopted in the program to prevent this type of behavior. It is noted when a value of f less than I is first reached, and then the plastic strain increments are reduced by 10 percent successively until f reaches I from outside the yield surface. Actually, if f satisfies the tolerance criterion, the iteration loop is terminated.

After each calculation of the plastic strain increments, the new position of the cap must be computed. The cap parameter X is computed from equation (12) but the transcendental equation

$$C = X + R\alpha - Rye^{\beta C}$$

must be solved to obtain the value of C. A subroutine which incorporates Newton's iterative procedure is used to solve this transcendental equation. The other cap parameter (b) can be calculated once X and C are known.

The program computes new elastic and plastic strain components and stresses for each set of total strain subincrements. After these calculations have been completed for the total number of subincrements, a new set of total

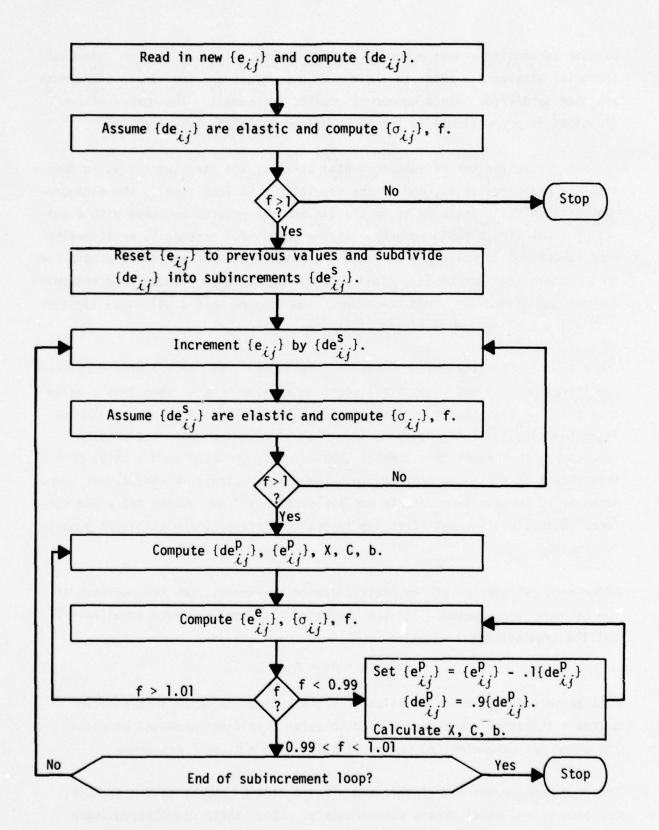


Figure 4. Flowchart of One Cycle of Total Strain Increment Procedure for Soil Cap Model

strains is read in and the total strain increment procedure is repeated. A flowchart describing the essential features of the total strain increment procedure for a soil cap constitutive model is shown in figure 4.

The soil cap model was implemented in the one-dimensional, wave-propagation code, WONDY IV (ref. 6). Since this code utilizes the total strain increment approach, the essential features of ELLSTR were directly incorporated in the WONDY IV Code. However, modifications were made in the coding to account for the absence of shear strains in one-dimensional motion.

Lawrence, R. J., and Mason, D. S., WONDY IV - A Computer Program for One-Dimensional Wave Propagation with Rezoning, SC-RR-71-0284, Sandia Laboratories, Albuquerque, New Mexico, August 1971.

# SECTION IV COMPARATIVE RESULTS

#### McCORMICK RANCH SAND

Results obtained with the specific cap model were compared with the behavior of real geologic materials. Since data were available for McCormick Ranch sand (refs. 7 and 8) Weidlinger Associates determined the cap model parameters for this material from the uniaxial strain, triaxial stress, and hydrostatic data. DiMaggio and Sandler (ref. 5) used these data to estimate the following cap parameters for McCormick Ranch sand:

 $\alpha$  = 250 psi (1.72 MPa) R = 2.5  $\beta$  = 6.7 x 10<sup>-4</sup>/psi (9.7 x 10<sup>-8</sup>/Pa) D = 6.7 x 10<sup>-4</sup>/psi (9.7 x 10<sup>-8</sup>/Pa)  $\gamma$  = 180 psi (1.24 MPa) W = 0.066

Young's modulus, E, and Poisson's ratio,  $\nu$ , were estimated to be 100 ksi (689 MPa) and 0.25, respectively. The laboratory data did not show a noticeable elastic region upon initial loading; therefore, the value of the cap parameter Z was arbitrarily chosen to be -5 psi (-0.034 MPa). These parameters were used in ELLSTR to simulate uniaxial strain and hydrostatic behavior.

Figure 5 shows a comparison of the experimental data and the cap model results for uniaxial strain and hydrostatic tests. These cap model results compare quite well with the laboratory uniaxial material behavior, although there is a noticeable difference in the two responses in the unloading portion of the test. The laboratory data exhibit a more predominant recovery of strain than do the cap model results. Weidlinger Associates reported that the hydrostatic data

Zelasko, J. S., and Ingram, J. K., Soil Property Investigation and Free-Field Ground Motion Measurements, Project BACKFILL, USAEWES, Vicksburg, Mississippi, December 1967.

<sup>8.</sup> Mazanti, B. B., and Holland, C. N., Study of Soil Behavior Under High Pressure, Report 1: Response of Two Recompacted Soils to Various States of Stress, Report S-70-2, USAEWES, Vicksburg, Mississippi, February 1970.

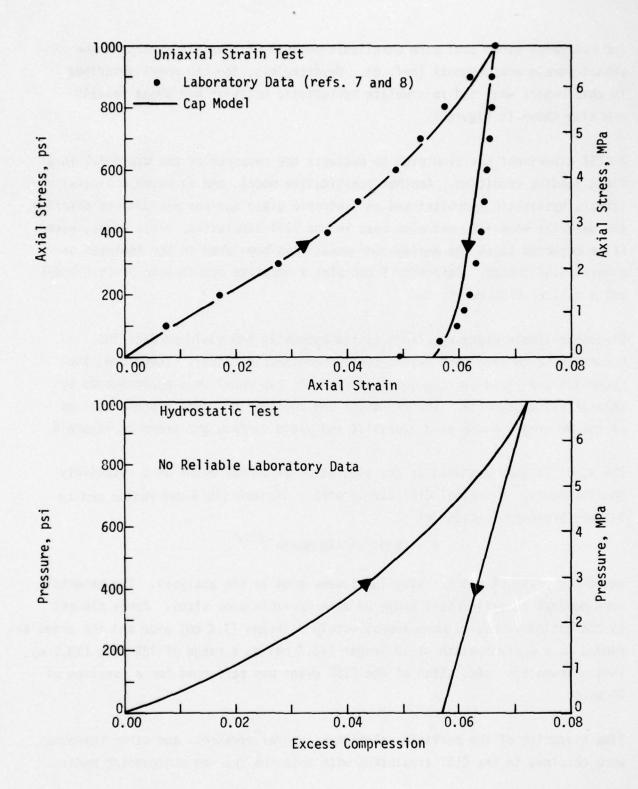


Figure 5. Comparison of Cap Model and Laboratory Data for McCormick Ranch Sand

for McCormick Ranch sand were unreliable because of possible errors in the radial strain measurements (ref. 5). Nevertheless, the cap model described in this report was used to simulate hydrostatic behavior and these results are also shown in figure 5.

A CIST experiment was simulated to evaluate the response of the cap model in a field loading condition. Another constitutive model, one in which a piecewise linear, hysteretic hydrostat and an isotropic yield surface are used to describe the material behavior, was also used in the CIST simulation. This model, hereafter referred to as the *engineering model*, has been used in the analyses of several CIST events. Reference 9 contains a complete description of this model and a typical CIST event.

Piecewise linear representations of the hydrostat and yield surface for McCormick Ranch sand were needed for the engineering model. Therefore, the hydrostat and yield surface obtained from the cap model were approximated by straight-line segments. The cap model and engineering model representations of the McCormick Ranch sand hydrostat and yield surface are shown in figure 6.

The WONDY IV Code was used in the simulation of a CIST event at a relatively shallow depth. A typical CIST cavity with a 12-inch (30.5-cm) radius and an assumed pressure function of

$$P = 5800 \text{ psi } (40 \text{ MPa})e^{-120t}$$

where P = pressure and t = time (sec) were used in the analysis. The materials were modeled in cylindrical geometry with variable zone sizes. Zones closest to the explosive cavity were approximately 3 inches (7.6 cm) wide and the zones expanded to a maximum width of 18 inches (45.7 cm) at a range of 125 feet (38.1 m). This mathematical simulation of the CIST event was performed for a duration of 20 msec.

Time histories of the particle velocities, radial stresses, and other responses were obtained in the CIST simulation with both the cap and engineering models.

<sup>9.</sup> Bratton, J. L., Fedock, J., and Higgins, C. J., A Parametric Study of the Effects of Material Properties Upon Cylindrical Wave Propagation, AFWL Technical Note (in preparation).

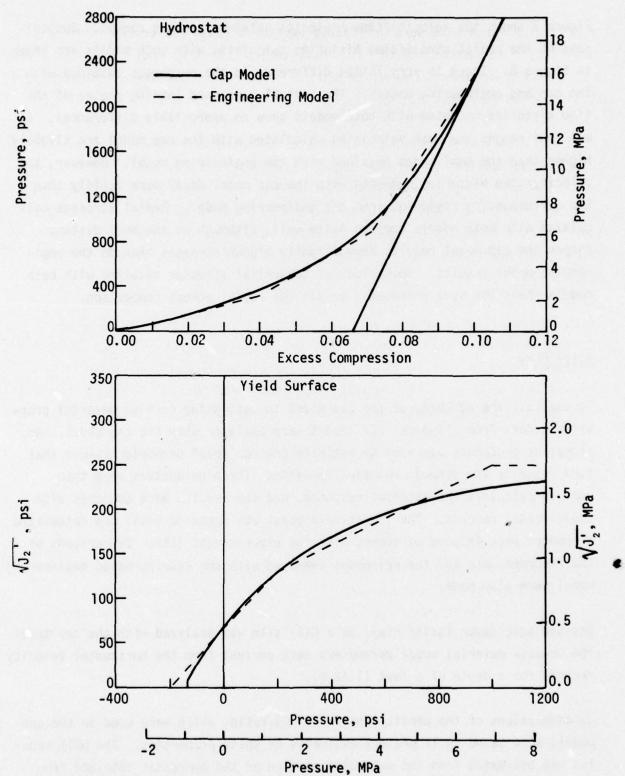


Figure 6. Comparison of Cap and Engineering Model Representations of McCormick Ranch Sand Properties

Figure 7 shows the velocity/time histories obtained at four ranges. Comparisons of the radial stress/time histories calculated with both models are shown in figure 8. There is very little difference in the responses obtained with the cap and engineering models. The arrival times and loading phases of the time histories computed with both models show no appreciable differences. At all four ranges the peak velocities calculated with the cap model are slightly higher than the amplitudes obtained with the engineering model. However, the velocity/time histories computed with the cap model decay more rapidly than the corresponding responses from the engineering model. Radial stresses calculated with both models compare quite well, although at the more distant ranges the cap model results show slightly higher stresses than do the engineering model results. Comparison of tangential stresses obtained with both models shows the same phenomenon as did the radial stress comparison.

#### STIFF CLAY

To evaluate the adequacy of the cap model in estimating in-situ material properties, data from a typical CIST event were analyzed with the cap model. An iterative procedure was used to estimate the cap model parameter values that best describe the dynamic material behavior. These parameters were then used to calculate the material response, and the results were compared with experimental records. The iterative process was repeated until the calculated responses were in good agreement with the experimental data. Comparisons of the recorded data and the responses computed with the in-situ-based engineering model were also made.

One geologic layer (stiff clay) at a CIST site was analyzed with the cap model. The in-situ material model parameters were derived from the horizontal velocity records for a depth of 5 feet (1.52 m).

In-situ values of the density and Poisson's ratio, which were used in the cap model, were based on laboratory estimates of these properties. The bulk modulus was estimated from the unloading portion of the hydrostat obtained from laboratory data. Initial estimates of cap parameters D and W were obtained by determining a best fit to the loading portion of the laboratory hydrostat. The value of R was chosen to be 4.0. Since laboratory estimates were available

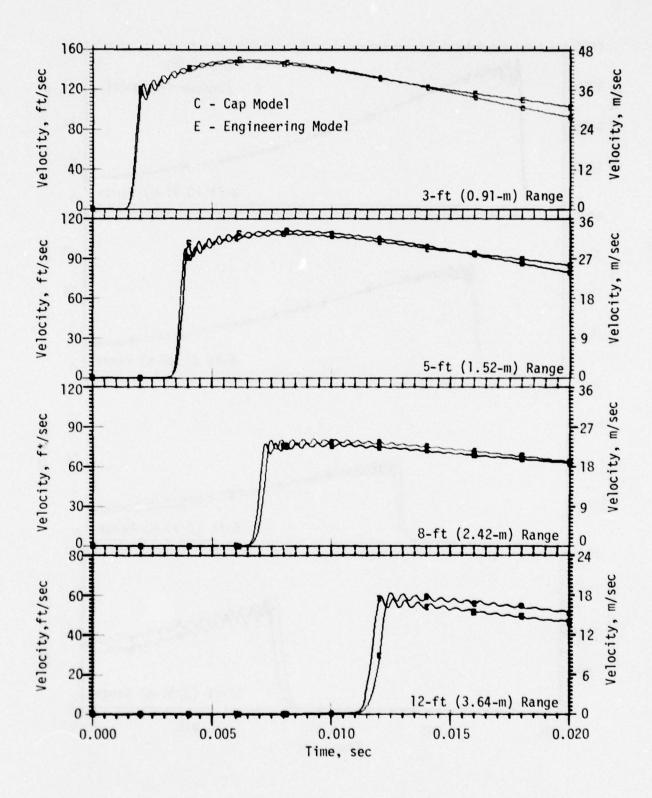


Figure 7. Comparison of Velocity/Time Histories from Cap and Engineering Model Representations of McCormick Ranch Sand

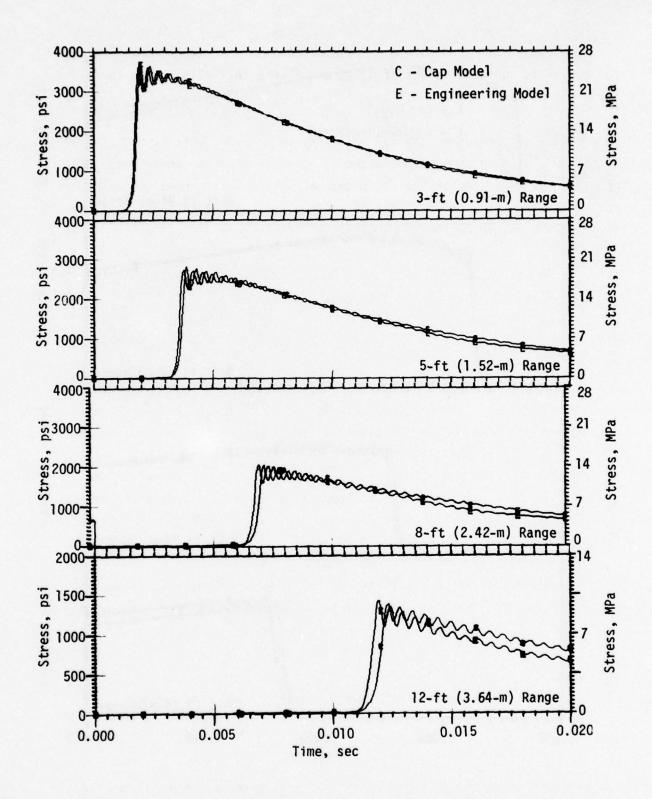


Figure 8. Comparison of Radial Stress/Time Histories from Cap and Engineering Model Representations of McCormick Ranch Sand

for the yield surface, values of  $\alpha$ ,  $\beta$ , and  $\gamma$  were initially chosen to fit these yield data.

Once initial estimates of the cap model parameters were established, the WONDY IV Code was used to compute the material response based on an assumed input pressure function. After the cap model parameters were varied several times during the iterative process, the parameters which produced the best fit to the experimental velocities were obtained. These were as follows:

$$\alpha$$
 = 46 psi (0.32 MPa) D = 4.0 x 10<sup>-4</sup>/psi (5.8 x 10<sup>-8</sup>/Pa)  
 $\beta$  = 2.5 x 10<sup>-3</sup>/psi (3.6 x 10<sup>-7</sup>/Pa) W = 0.040  
 $\gamma$  = 12 psi (0.08 MPa)  $\nu$  = 0.32  
 $R$  = 4.0 K = 2.6 x 10<sup>5</sup> psi (1790 MPa)

The responses obtained with the initial estimates of the cap model parameters compared fairly well with the experimental data; i.e., the final estimates of many parameters were not significantly different from their initial values. In particular, only D and W, which were initially estimated to be  $1.0 \times 10^{-3}$ / psi (1.45 x  $10^{-7}$ /Pa) and 0.031, respectively, were greatly varied in the iterative process. A similar iterative process was used to estimate the parameters for the engineering model, which was also used to describe the in-situ behavior of the stiff clay.

Tensile properties of the stiff clay could not be absolutely determined because, in general, the CIST event did not produce material responses with noticeable tensile phases. Hence, no tensile properties of the stiff clay were estimated.

In both iterative processes the assumed input pressure function was

$$P = 5800 \text{ psi } (40 \text{ MPa})e^{-450t}$$

The geometric modeling of the material for both cases was the same as that described previously for the McCormick Ranch sand. A simulation time of 30 msec was used for both.

Final estimates of the cap model parameters, which described the clay material at the 5-foot (1.52-m) depth, were used as input to ELLSTR. Hydrostatic behavior was simulated in the program and the results were compared with the hydrostats obtained with the in-situ engineering model and the laboratory-inferred properties (fig. 9). The cap model parameters ( $\alpha$ ,  $\beta$ , and  $\gamma$ ) were used to describe the final estimate of the yield surface. A comparison of the estimated in-situ yield surfaces obtained with the cap and engineering models and the laboratory-based properties is also shown in figure 9.

Velocity/time histories calculated with the cap and in-situ-based engineering models are compared with the experimental records in figures 10 and 11, respectively. A comparison between the responses calculated with the laboratory-based engineering model and the field records is shown in figure 12.

Arrival times calculated with both in-situ models are in good agreement with the field data. Peak velocities computed with the cap model are lower than the corresponding amplitudes calculated with the engineering model. The loading phases and peak velocities calculated with the cap model match the experimental data quite well at the 3-foot (0.91-m) and 5-foot (1.52-m) ranges, but the computed amplitude is approximately 40 percent higher than the recorded amplitude at the 8-foot (2.42-m) range. Neither in-situ model gives a good representation of the actual material behavior at the 8-foot (2.42-m) range. The unloading portions of the time histories calculated with both in-situ models compare reasonably well with the experimental data. In general, the differences between the responses calculated with both in-situ models are not significant.

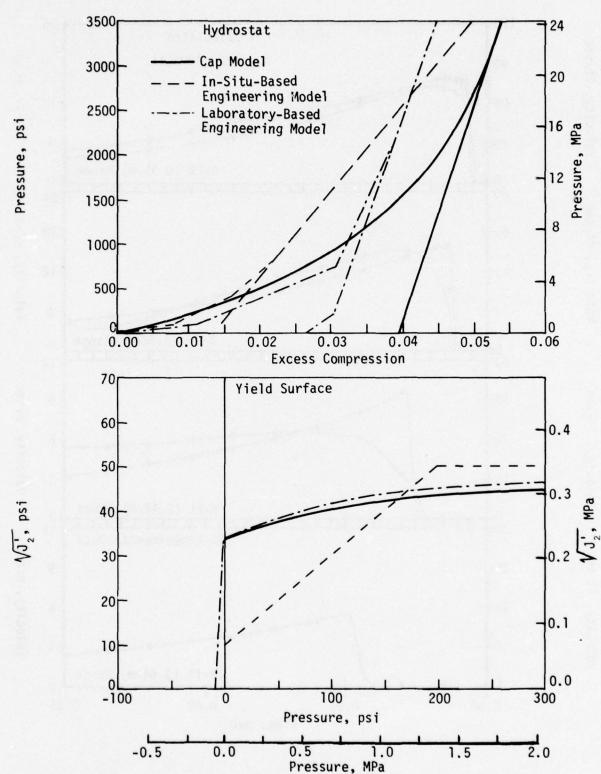


Figure 9. Comparison of Cap and Engineering Model Representations of In-Situ Properties and Laboratory-Inferred Properties for Stiff Clay

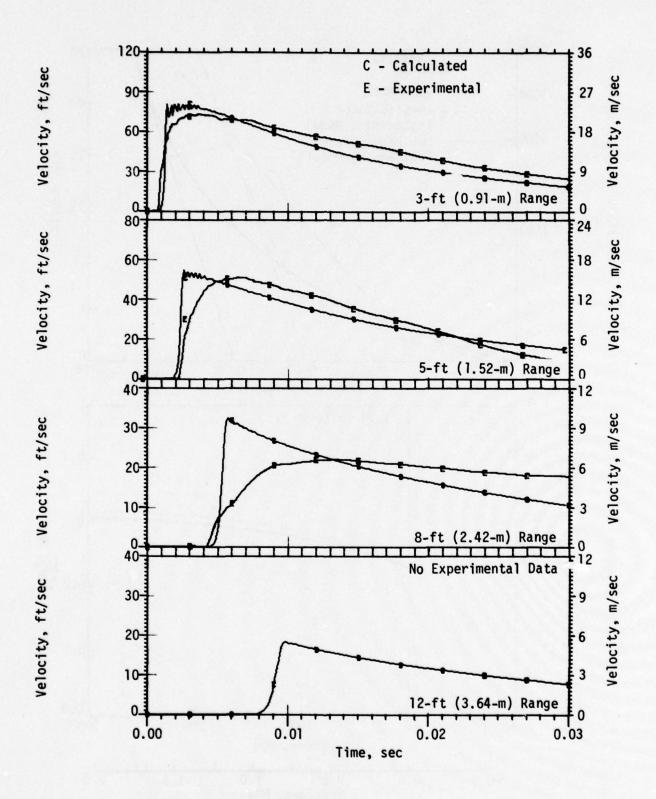


Figure 10. Comparison of Velocity/Time Histories from Estimated In-Situ Cap Model Parameters and CIST Data for Stiff Clay

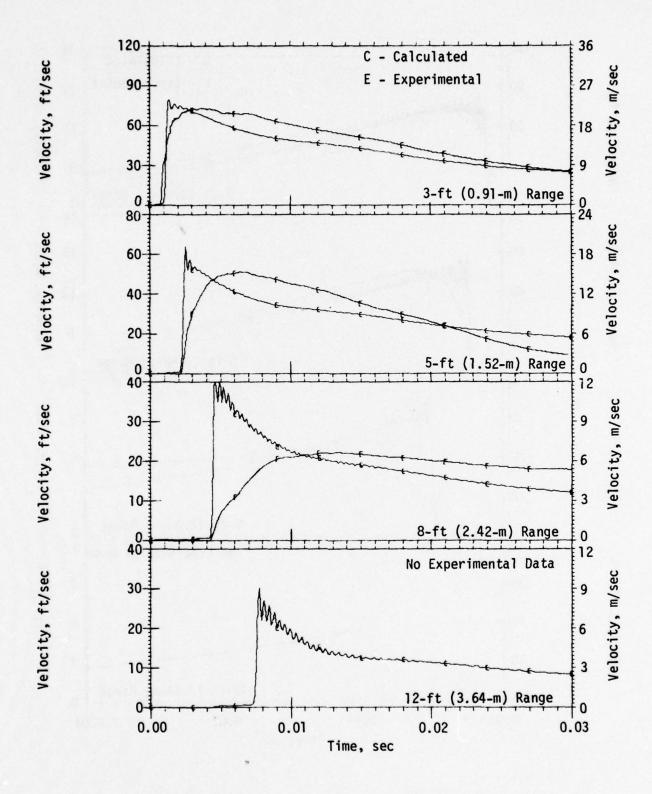


Figure 11. Comparison of Velocity/Time Histories from Estimated  $In\mbox{-}Situ$  Engineering Model Parameters and CIST Data for Stiff Clay

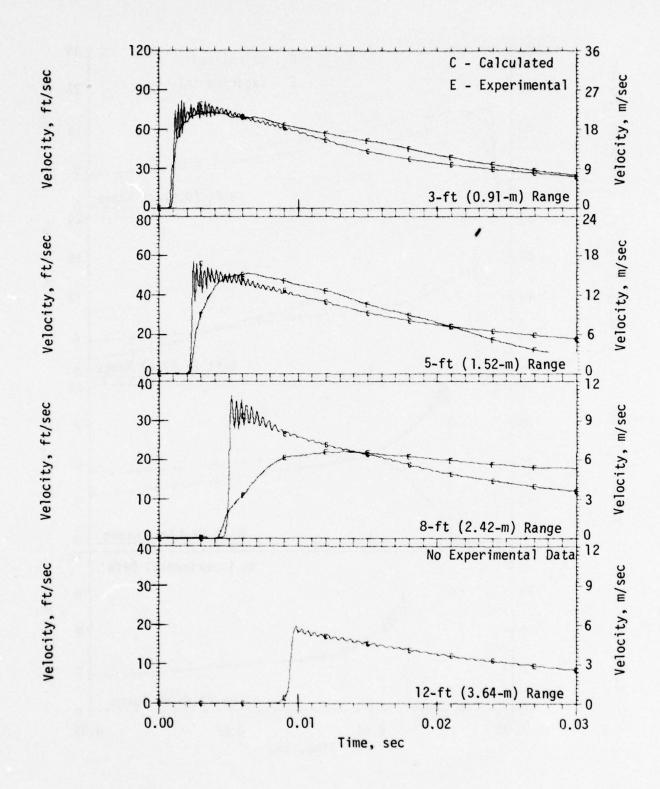


Figure 12. Comparison of Velocity/Time Histories from Laboratory-Based Engineering Model Parameters and CIST Data for Stiff Clay

# SECTION V CONCLUSIONS AND RECOMMENDATIONS

The cap model is capable of representing laboratory and dynamic in-situ behavior for at least two distinct geologic materials. Results from an analysis of a CIST event show that the cap model can be used to produce velocity/time histories that are in reasonably good agreement with experimental data.

The cap model meets all uniqueness and stability requirements. (The theoretical basis for the cap model is described in reference 5.) Since the cap model utilizes an associated flow rule with a convex yield surface, it satisfies Drucker's stability postulate; the engineering model uses a nonassociated flow rule and does not satisfy the postulate.

The cap model described in this report and implemented in the WONDY IV Code has several disadvantages, however. The procedure for fitting both laboratory and field data is fairly complex. A trial-and-error process is required to determine values of the cap model parameters, but recent studies (refs. 10 and 11) have indicated that the iterative procedure can be automated. It is also difficult to relate the cap model parameters to the material properties in commonly understood terms. The cap model equation-of-state is more complex than the equation-of-state based on the engineering model. However, the required execution times for the calculations performed in this study were not appreciably different for the two models.

Some aspects of typical CIST responses are difficult to reproduce with the cap model, but this difficulty is common to the engineering model. The CIST data often

Isenberg, J., Collins, J. D., and Kennedy, B., Statistical Estimations of Geological Material Model Parameters from Cylindrical In-Situ Test Data, AFWL-TR-76-187, Air Force Weapons Laboratory, Kirtland Air Force Base, New Mexico.

<sup>11.</sup> Isenberg, J., Automated Data Analysis Application of Statistical Estimation of Geological Material Model Parameters, AFWL Technical Report (in preparation).

show velocities that maintain high amplitudes for relatively long durations, and both the cap and engineering models have difficulty in matching this type of behavior. Additionally, many CIST velocity records show a sharp decrease in amplitude after the initial peak, followed by a gradual increase in the velocity over several milliseconds. This behavior is also difficult to match with either the cap or engineering model. The tensile behavior of soils is an area of much uncertainty, and neither the cap nor the engineering model appears to give a completely adequate representation of this type of behavior.

For the cases considered in this study, it appears that if the cap model parameters were chosen to match the hydrostat and yield surface of the engineering model, the differences between the time histories calculated with both models would be minimal. This suggests that other approaches to the modeling of dynamic soil behavior need to be considered. The use of a residual yield surface may be one means for obtaining the desired waveform behavior.

Although the cap model satisfies all theoretical requirements and can adequately represent most types of static and dynamic soil behavior, it does not appear that the cap model offers significant advantages over the engineering model for the cylindrical cases evaluated. However, the guarantee of solution uniqueness that is ensured by the cap model may provide the user with increased confidence when problems involving general three-dimensional conditions are calculated.

## APPENDIX A PROGRAM ELLSTR

#### INPUT REQUIREMENTS

Card 1 - Format (8A10)
Title Card (up to 80 characters)

Card 2 - Format (10F8.2) Material Constants - E,  $\nu$ , D, W, R,  $\alpha$ ,  $\beta$ ,  $\gamma$ , Z Subincrement Control - PINC

Card 3 to Last Card - Format (IIO, 6FI0.2) - NSTEP,ET(I)

NSTEP is an integer to identify each set of total strains that is read in. Normally, the first card of this set will have NSTEP = 0, and ET(I) = 0., 0., 0., 0., 0., 0. Subsequent values of total strain define the prescribed total strain path.

NSTEP = -1 indicates that this set is complete and that another problem set is next in line.

NSTEP = -2 indicates that this set is the last complete problem set.

ET(I) = components of total strain.

```
PROGRAM ELLSTR(INPUT.OUTPUT.TAPE5=INPUT.TAPE6=OUTPUT)
COMMON /STRESS/SIG(6).SD1.SD2.SD3.FJ1.FJ2P.FJ2PR
       COMMON /STRAIN/EPPL(6) .EEL(6) .ET(6) .DET(6) .DEPL(6) .EP1
       COMMON /MATER/C2 . C3 . G2 . CC (6 . 6) . ALPH . BET . GAM . R . D . W
       COMMON /CAP/X.C.DW.RSQ.RB.RBSQ.RALPH.RGAM.GMBET
       COMMON /CONTRL/NCOUNT . XZ . CHISQ . FY . NDUM
C
       DIMENSION TITLE(10) . ETNEW(6)
       THIS PROGRAM ASSUMES A STRAIN INCREMENT PRESCRIBED PATH ALL SIX INDEPENDENT COMPONENTS OF TOTAL STRAIN ARE REQUIRED
 10 READ(5.1000)(TITLE(1).1=1.8)
1000 FORMAT(8A10)
       READ(5.1010)E.FNU.D.W.R.ALPH.BET.GAM.XINT.PINC
 1010 FORMAT(10F8.2)
WRITE(6.1100)(TITLE(1).1=1.8)
 1100 FORMAT(1H1.10X.8A10/)
       WRITE(6.1110)E.FNU.D.W.R.ALPH.BET.GAM.XINI.PINC
 1110 FORMAT(IH +3X+2HE=+E8-2+3X+3HNU=+F4+2+3X+2HD=+E8-2+3X+2HW=+F6-4+

1 3X+2HR=+F6-2+3X+6HALPHA=+F6-1+3X+5HBETA=+E8+2+3X+6HGAMMA=+F6-1+

2 3X+5HXINT=+F5-1+3X+5HPINC=+F5-1/)
       INITIALIZE VARIABLES
       CHISQ=(0.9/BET) *ALOG(ALPH/GAM)
       FK=ALPH-GAM
       DW=D#W
       RSQ=R#R
       RALPH=R*ALPH
        RGAM=R*GAM
        GMBFT=GAM*BET
        X=XINT
        XRA=X+RALPH
       C=0.1
CALL COMPCIC.XRA.RGAM.BET)
       RB=C-X
       RBSQ=RB*RB
       XSQ=X+X
G2= E/(1.+FNU)
       C1=G2/(1.-2.*FNU)
       C2=C1*(1.-FNU)
        C3=C1 *FNU
       FP1=0.
       FY=FJ1=FJ2PR=0.
        NINC=0
       NCOUNT=0
DO 15 I=1.6
       SIG(1)=0.
       FT(1)=0.
        FEL (1)=0.
       EPPL(1)=0.
DO 15 J=1.6
    15 CC(1.J)=0.
       DO 20 1=1+3
   00 20 J=1.3
20 CC(1.J)=C3
       DO 22 1=1.3
    22 CC(1+1)=C2
    24 CC(1.1)=G2
       STRAIN INCREMENT CYCLE. READ NEW TOTAL STRAINS
 50 READ(5.1050)NSTEP.(ETNEW(1).I=1.6)
1050 FORMAT(110.6F10.2)
        IFINSTEP.EQ.OIGO TO 700
        IFINSTEP.EQ.-11GO TO 10
        IFINSTEP.EQ .- 21STOP
       NCOUNT = 0
        COMPUTE TOTAL STRAIN INCREMENTS. ASSUME ELASTIC AND COMPUTE STRESSES.
        DO 60 1=1.6
        DET(I)=ETNEW(I)-ET(I)
    60 ET(T)=ETNEW(T)
3
        CHECK FOR YIELDING. IF(FY.LE.1) INCREMENT IS ELASTIC
```

```
NINC=0
       NDUM=0
CALL YIELD
        IF(FY.LE.1.)GO TO 700
c
       REDUCE SIZE OF TOTAL STRAIN INCREMENTS
       NINC=(FY-1.)*PINC
       IF(NINC . GT . 2000 ) NINC = 2000
       IF(NINC.LT.1)NINC=1
        FINC=NINC
       DO 100 I=1.6
ET(1)=ET(1)-DET(1)
  100 DET(1)=DET(1)/FINC
C
       PROCEED WITH THE SMALL TOTAL STRAIN INCREMENTS
       DO 150 K=1+NINC
  00 150 I=1+6
110 ET(I)=ET(I)+DET(I)
CALL YIELD
IF(FY+LE-1+0)GO TO 150
       CALL PSTRN
       NINNER=0
  113 CALL YIELD
       0.99 .LE. FY .LE. 1.01 IMPLIES SATISFACTORY STRESS POINT IF(FY.GT.1.01)GO TO 127 IF(FY.GT.0.99) GO TO 150
C
       NINNER=NINNER+1
       IF(NINNER.GT.100) GO TO 150
       DO 126 1=1.6
        FACT = -0 . 1
  EPPL(1)=EPPL(1)+FACT*DEPL(1)
126 DEPL(1)= 9*DEPL(1)
EP1=EPPL(1)+EPPL(2)+EPPL(3)
       X=XINT+(ALOG(1.0+EP1/W))/D
XRA=X+RALPH
       CALL COMPC(C+XRA+RGAM+BET)
       RBSQ=RB*RB
       GO TO 113
  127 NINNER=NINNER+1
140 CALL PSTRN
       GO TO 113
  150 CONTINUE
  700 WRITE(6.1150)NSTEP.NINC.NCOUNT
1130 FORMAT(1H +/+5X+6HNSTEP=+15+5X+5HNINC=+15+5X+7HNCOUNT= +15)
       FMU=ET(1)+ET(2)+ET(3)
WRITE(6+1140)(ET(1)+I=1+6)+FMU
 1140 FORMAT(1H .4X.12HTOTAL STRAIN.4X.6E10.3.5X.3HMU=.E10.3)
       WRITE(6.1130)(EEL(I).I=1.6)
 1130 FORMAT(1H +4X+14HELASTIC STRAIN+2X+6E10+3)
 WRITE(6+1125)(EPPL(1)+1=1+6)+EP1
1125 FORMAT(1H +4X+14HPLASTIC STRAIN+2X+6E10+3+5X+4HEP1=+E10+3)
 WRITE(6+1120)(SIG(1)+1=1+6)+FJ1+FJ2PR
1120 FORMAT(1H +10X+6HSTRESS+4X+6E10+3+5X+3HJ1=+E14+5+>X+6HFJ2PR=+E14+5
C
       B=SQRT(RBSQ)/R
       WRITE(6.1122)FK.B.C.X.FY
 1122 FORMAT(1H +4X+2HY=+E10+3+5X+2HB=+E10+3+5X+2HC=+E10+3+5X+2HX=+
      1 E10.3.5X.3HFY=.E10.3)
C
       GO TO 50
       STOP
```

```
SURROUTINF PSTRN
          SURROUTINF PSTRN
COMMON /STRESS/SIG(6) +SD1+SD2+SD3+FJ1+FJ2P+FJ2PR
COMMON /STRAIN/EPPL(6) +EEL(6)+ET(6)+DET(6)+DEPL(6)+EP1
COMMON /MATER/C2+C3+G2+CC(6+6+ALPH+BET+GAM+R+D+#
COMMON /CAP/X+C+DW+RSQ+RB+RBSQ+RALPH+RGAM+GMBET
          COMMON /CONTRL/NCOUNT . XZ . CHISQ . FY . NDUM
C
           DIMFNSION GF (6)
          GF=GRADIENT OF F WRT STRESS
GFS=GRADIENT OF F WRT STRAIN
          NCOUNT = NCOUNT+1
C
           IFIFJ1.GT.C) GO TO 20
          YIELDING ON CAP (F2)
          COMPUTE GF
          A1=FJ1-C
A22=2.*A1
           A23=RSQ/RBSQ
           A24=A22/RBSQ
          A25=2. #A23
GF(1) = A23 * SD1+A24
          GF(1)=A23*SD2+A24
GF(2)=A23*SD2+A24
GF(3)=A23*SD3+A24
GF(4)=A25*SIG(4)
GF(5)=A25*SIG(5)
          GF(6)=A25*SIG(6)
          COMPUTE GFS
          A12=X-C
A3=A1+FY*RB*BET*(RB-RALPH)
          A4=RBSQ*DW*(1.+BET*(RALPH+A12))
GFSS=-2.*EXP(-D*(X-XINT))*A3/A4
C
     B3=0.

D0 10 I=1.3

10 B3=B3+GF(1)*GFSS
          GO TO 30
C
          YIELDING ON FI
     ?n 83=n.
          COMPUTE GF
          A5=FY/(2. #FJ2P)
          A6=2.*A5*FY*GMBET*FJ2PR*EXP(BET*FJ1)
          GF(1)=A5*SD1+A6
GF(2)=A5*SD2+A6
          GF(3)=A5*SD3+A6
A7=2.*A5
          GF(4)=A7#SIG(4)
GF(5)=A7#SIG(5)
          GF(6)=A7*SIG(6)
          COMPUTE DLAM
     30 A)=0.
          B2=0.
    DO 40 1=1+3

DO 40 J=1+3

B1=B1+CC(I+J)*DET(I)*GF(J)

40 B2=B2+CC(I+J)*GF(I)*GF(J)
     DO 50 1=4+6
B1=B1+2+*CC([+])*DET([])*GF([)
50 B2=B2+CC([+])*GF([))*GF([)
          DLAM=81/(82-83)
```

```
COMPUTE PLASTIC STRAIN
        DO 60 1=1+6
DEPL(1)=DLAM*GF(1)
EPPL(1)=EPPL(1)+DEPL(1)
EP1=EPPL(1)+EPPL(2)+EPPL(3)
    60
         X=XINT+(ALOG(1.0+EP1/W))/D
         XRA=X+RALPH
         CALL COMPCIC+XRA+RGAM+BET)
         RBSQ=RB#RB
         RETURN
         END
        SUBROUTINE YIELD
        COMMON /STRESS/SIG(6).SD1.SD2.SD3.FJ1.FJ2P.FJ2PR
COMMON /STRAIN/EPPL(6).EEL(6).ET(6).DET(6).DEPL(6).EP1
COMMON /MATER/C2.C3.G2.CC(6.6).ALPH.BET.GAM.R.D.W
         COMMON /CAP/X.C.DW.RSQ.RB.RBSQ.RALPH.RGAM.GMBET
        COMMON /CONTRL/NCOUNT . XZ . CHISQ . FY . NDUM
        COMPUTE ELASTIC STRAINS AND STRESSES.
        NO 10 I=1+6

EEL(I)=ET(I)=EPPL(I)

SIG(1)=C2*EEL(1)+C3*(EEL(2)+EEL(3))

SIG(2)=C2*EEL(2)+C3*(EEL(3)+EEL(1))
    10
        SIG(3)=C2*EEL(3)+C3*(EEL(1)+EEL(2))
         SIG(4)=G2*EEL(4)
         51G(5)=G2*EEL(5)
         516(6)=G2*EEL(6)
         FJ1=SIG(1)+SIG(2)+SIG(3)
         FJ3=FJ1/3.
SD1=SIG(1)-FJ3
         SD2=516(21-FJ3
         SD3=SIG(3)-FJ3
       FJ2P=(SD1*SD1+SD2*SD2+SD3*SD3)/2.+
1 (S[G(4)**2)+(S[G(5)**2)+(S[G(6)**2)
FJ2PR=SQRT(FJ2P)
C
         1F(FJ1.GT.C) GO TO 20
        A=F.J1-C
        FY=(RSQ*FJ2P+A*A)/RBSQ
C
        IF(NDUM.EQ.O) FY=SORT(FY)
C
    20 IF(FJ1.GT.CHISQ)GO TO 30
DEN=ALPH-GAM*EXP(BET*FJ1)
         FY=(FJ2PR)/DEN
         RETURN
 30 PRINT 1000
1000 FORMAT(10X+24HWARNING ON F1 FROM YIELD )
         FJ1=0.
         FY=100.
         SUBROUTINE COMPC(C+C1+C2+C3)
        USE NEWTON'S METHOD
         COLD=C
    NC=0
70 A1=C2*EXP(C3*C)
        A2=C1-C-A1
        A3=C3+A1+1.
C=C+A2/A3
         IFIARSIC3+(COLD-C)).LT.0.0001)GO TO 90
        NC=NC+1
IF(NC.GT.201GO TO 80
        COLD=C
    GO TO 70
30 WRITE(6+1100)C
30 FORMAT(1H +4X+16HC NOT CONVERGING +E10+3)
         STOP
    90 IFIC.GT.0.01C=0.
        RETURN
         END
```

# APPENDIX B CAP MODEL EQUATION-OF-STATE SUBROUTINE

#### INPUT REQUIREMENTS

The input cards are essentially identical to those outlined in the WONDY manual. On Card 2 set NVAR = 28, and on Card 10 specify 2 for the equation-of-state. Cards 15 and 16 contain the equation-of-state constants and they are as follows:

Card 15 - Format (7E10)

CES (1, PLATE).....CES(7,PLATE) = initial mass density, initial bulk sound speed, Young's modulus, Poisson's ratio, alpha, beta, and gamma, respectively.

Card 16 - Format (7E10)

CES (8, PLATE).....CES(10, PLATE) = R, D, and W, respectively.

Note: The  $J_1$  coordinate of the initial cap has been set to  $.02\alpha$  in the program and subincrement control has been set to 20. Appropriate changes can be made in the coding to modify these set values.

In Subroutine GENERAT the values of C, X, and b must be preset by a call to STIN2 (entry point in STAT2) and stored in the appropriate locations in the vector STORE.

Subroutine STAT2 predicts stresses and strains based on the cap model equationof-state. In the first segment of the subroutine, the basic material constants are set up if a new material zone is involved, and then the previous values of stresses, strains, and cap coordinate data are recalled.

The standard WONDY procedure is followed in computing the strain rates, with the total strain increments and total strains evaluated next. Then the sub-routine closely follows ELLSTR with the exception that the evaluations performed by YIELD and PSTRN are incorporated directly into STAT2.

New values of stresses, strains, cap coordinates, and certain other variables are saved in the vector DATB before the return from the subroutine is made.

```
SUBROUTINE STAT2
WONDY IV+ BARON CAP MODEL
COMMON /CONST/ ADDATA(100)+B1+B2+CES(84+20)+EXIT+IALPHA+
  COMMON /JMSO/ DATB(100); DELRHO; DELXJ; JONE; NEWPLAT; RHODOT
COMMON /WJSD/ DEP; FCONST(20); FCONST(20); FCRIF(2U); FCRIF(2U);
L JTAPE; LDUMP; NSTART; SIGACT; SIGMAF(20); SIGMAIF(2U);
S SIGMAO(20); SIGMAOI(20); SIGSEP
   TYPE INTEGER PLATE, W4020
TYPE REAL KM, KT1, M, NOMESH
   SET UP VARIABLES FOR NEW PLATE
   IFINEWPLATIS.10
   RHON=CES(1.PLATE)
   CO=CES(2.PLATE)
   FNU=CES(4.PLATE)
   ALPH=CES(5.PLATE)
   RET=CES(6.PLATE)
   GAM=CES(7.PLATE)
   RR=CES(8.PLATE)
   D=CFS(9.PLATE)
   W=CFS(10.PLATE)
   DW=D+W
   RSQ=RR*RR
   RALPH=RR#ALPH
   RGAM=RR*GAM
   GMBFT=GAM*BET
   CHISQ=(0.9/BET) *ALOG(ALPH/GAM)
XZ=-0.02*ALPH
   G2=H/(1.+FNU)
   C1=G2/(1.-2.*FNU)
C2=C1*(1.-FNU)
C3=C1*FNU
   SET UP VARIABLES FOR ZONE
10 SIGX =- S
   SIGY=DATR(1)
   SIGZ=DATR(2)
   EEX=DATR(3)
EEY=DATR(4)
   EEZ=DATB(5)
   EPX=DATB(6)
EPY=DATB(7)
   FPZ=DATB(8)
   FTX=DATR(9)
   FTY=DATB(10)
   ETZ=DATR(11)
CB=DATR(12)
   XX=DATB(13)
   B=DATR(14)
   RB=RR*B
RBSQ=RB*RB
   COMPUTE STRAIN RATES
   DX=2.*(UN-UBN)/(DELXJ+X-XB)
    DZ=n.
    IF ( 1AI PHA . FQ . - 1 ) GO TO 20
    DY=2. + (UN+UBN)/(X+XB+XN+XBN)
    IF ( TALPHA . EQ. 1 ) DZ = DY
20 RHODOT = - DX-DY-DZ
    COMPUTE TOTAL STRAIN INCREMENTS AND STRAINS
   DELTT=DELT(1)
   DETX=DX*DELTT
    DETY=DY*DELTT
    DETZ=DZ*DELTT
    FTX=FTX+DFTX
    FTY=ETY+DETY
    FTZ=FTZ+DETZ
    SUPPOSE INCREMENT IS ELASTIC AND CHECK FOR YIELD
```

```
NINC=0
        FFX=ETX-EPX
EEY=ETY-EPY
        FEZ=ETZ-FPZ
         SIGX=C2*EEX+C3*(EEY+EEZ)
        $18X=63*EEX+63*(EEX+EEV)
        FJ1=SIGX+SIGY+SIGZ
        FJ3=FJ1/3.
SDX=SIGX-FJ3
        SDY=SIGY-FJ3
SDZ=SIGZ-FJ3
         FJ2P=0.5*(SDX*SDX+SDY*SDY+SDZ*SDZ)
        FJ2PR=SQRT(FJ2P)
         IFIFJ1.GT.CBIGO TO 30
         A=FJ1-CB
        FY=(RSQ+FJ2P+A+A)/RBSQ
        FY=SORT(FY)
•
    GO TO 32
30 IF(FJ1.GT.CHISQ) GO TO 31
FY=FJ2PR/(ALPH-GAM*EXP(BET*FJ1))
GO TO 32
31 FJ1=0.
        FY=100.
        CHECK FOR YIELDING
    32 IF(FY-LE-1-) GO TO 60
NIMC=(FY-1-)*20-
IF(NINC-GT-2000) NINC=2000
IF(NINC-LT-1) NINC=1
-
```

```
RETURN TO ORIGINAL STRAINS AND MAKE INCREMENTS SMALLER
ç
       ETX=ETX-DETX
        ETY=ETY-DETY
       ETZ=ETZ-DETZ
FINC=NINC
       DETX=DETX/FINC
       DETY=DETY/FINC
       DETZ=DETZ/FINC
5
       USE SMALLER TOTAL STRAIN INCREMENTS
C
       DO 55 INC=1.NINC
       ETZ=ETZ+DETZ
5
       CALCULATION OF YIELD FUNCTION VALUE
    34 EEX=ETX-EPX
       EEY=ETY-EPY
       FEZ=FTZ-EPZ
SIGX=C2*EEX+C3*(EEY+EEZ)
        SIGY=C2*EEY+C3*(EEZ+EEX)
        SIGZ=CZ*EEZ+C3*(EEX+EEY)
        FJ1=SIGX+SIGY+SIGZ
       FJ3=FJ1/3.
SDX=SIGX-FJ3
SDY=SIGY-FJ3
SDZ=SIGZ-FJ3
       FJ2P=0.5*(SDX*SDX+SDY*SDY+SDZ*SDZ)
FJ2PR=SQRT(FJ2P)
       IF(FJ1.GT.CB)GO TO 36
A=FJ1-CB
FY=(RSQ*FJ2P+A*A)/RBSQ
        GO TO 38
    36 IF(FJ1.GT.CHISQ) GO TO 37
FY=FJ2PR/(ALPH-GAM*EXP(BET*FJ1))
       GO TO 38
    37 FJ1=0.
    38 CONTINUE
```

```
-
        IF(FY.LE.1.0) GO TO 55
       CALCULATE PLASTIC STRAINS
C
    39 IF(FJ1.GT.CB) GO TO 40
        YIELDING ON CAP (F2)
       A1=1./(B*B)
A2=2.*(F)1-CB)/RBSQ
BB3=-3.*A2*EXP(-D*(XX-XZ))*(A2+2.*F/*BET*(1.-ALPH/B))/
1 (DW*(1.*BET*(RALPH-CB+XX)))
       GO TO 50
ç
        YIELDING ON FI
    40 A1=FY/(2.*FJ2P)
        A2=2.*A1*FY*GMBET*FJ2PR*EXP(FJ1*BET)
        BB3=0.
        COMPUTE GRADIENTS WRT STRESS
    50 GFX=A1*SNX+A2
        GFZ=A1*SDY+A2
GFZ=A1*SDZ+A2
C
        CGFX=C2*GFX+C3*(GFY+GFZ)
CGFY=C2*GFY+C3*(GFZ+GFX)
        CGFZ=C2*GFZ+C3*(GFX+GFY)
        BB1=CGFX*DETX+CGFY*DETY+CGFZ*DETZ
BB2=CGFX*GFX+CGFY*GFY+CGFZ*GFZ
DLAM=BB1/(BB2~BB3)
        COMPUTE NEW PLASTIC STRAINS
        DEPX=DLAM#GFX
        DEPY=DLAM#GFY
DEPZ=DLAM#GFZ
        FPX=FPX+DEPX
        EPY=EPY+DEPY
        EPZ=EPZ+DEPZ
        EP1=EPX+EPY+EPZ
        NINNER=0
C
        ARG=1.0+EP1/W
        IF (ARG.LE.0.0) GO TO 112
        XX=XZ+(ALOG(1.0+EP1/W))/D
        XRA=XX+RALPH
CALL COMPC(CB+XRA+RGAM+BET)
        B=1CB-XX1/RR
        RB=CB-XX
        RBSQ=RB#RB
        GO TO 113
  112 EEX=ETX-EPX
EEY=ETY-EPY
        EEZ=ETZ-EPZ
        SIGX=CZ*EEX+C3*(EEY+EEZ)
        SIGY=C2*EEY+C3*(EEZ+EEX)
SIGZ=C2*EEZ+C3*(EEX+EEY)
        FJ1=SIGX+SIGY+SIGZ
        CB*FJ1
B*ALPH-GAM*EXP(BET*FJ1)
RB*RR*B
        RBSQ=RB#RB
        XX=CB-RB
GO TO 114
        CALCULATE YIELD FUNCTION WITH NEW VALUES OF PLASTIC STRAIN
  113 EEX=ETX-EPX
EEY=ETY-EPY
```

```
STGX=CZ*EEX+C3*(EEY+EEZ)
        SIGY=C2*EEY+C3*(EEZ+EEX)
SIGZ=C2*EEZ+C3*(EEX+EEY)
        FJ1=SIGX+SIGY+SIGZ
  114 FJ3=FJ1/3.
SDX=SIGX-FJ3
        SDY=SIGY-FJ3
        SDZ=SIGZ-FJ3
        FJ2P=0.5*(SDX*SDX+SDY+SDY+SDZ*SDZ)
        FJ2PR=SQRT(FJ2P)
•
        1F(FJ1.GT.CB) GO TO 48
        A=FJ1-CB
       FY=(RSQ#FJ2P+A*A)/RBSQ
GO TO 41
    48 IF(FJ1.GT.CHISQ) GO TO 49
        FY=FJ2PR/(ALPH-GAM*EXP(BET*FJ1))
        GO TO 41
    49 FJ1=0.
FY=100.
    41 CONTINUE
        0.99.LE.FY.LE. 1.01 IMPLIES SATISFACTORY STRESS PUINT.
5
        IF(FY.GT.1.01)GO TO 39
IF(FY.GT.0.99)GO TO 55
c
        THIS PORTION OF THE ITERATION PREVENTS OSCILLATIONS ABOUT A POINT
       ON THE YIELD SURFACE. PLASTIC DEFORMATION HAS OCCURRED BUT FY .LT.0.99. REDUCE PLASTIC STRAINS TO APPROACH YIELD SURFACE
C
        FROM EXTERIOR.
C
        NINNER=NINNER+1
        IF(NINNER.GT.50) GO TO 55
        FACT =- 0 . 1
FPX = EPX + FACT + DEPX
        EPY=EPY+FACT+DEPY
        EPZ=EPZ+FACT+DEPZ
        DEPX=0.9*DEPX
       DEPY=0.9*DEPY
DEPZ=0.9*DEPZ
        FP1=FPX+FPY+FPZ
        ARG=1.+EP1/W
       IF(ARG.LE.0.0) GO TO 112
XX=XZ+(ALOG(1.0+EP1/W))/D
        XRA=XX+RALPH
       CALL COMPC(CB.XRA.RGAM.BET)
B=(CB-XX)/RR
        RB=RR+B
        RASQ=RA#RB
-
    55 CONTINUE
    60 CONTINUE
C
        STORE NEW VARIABLES
        SN=-SIGX
        PN=_SIGX-SIGY-SIGZ
        ZN=SIGX-SIGY
        FN=F
       CN=CO
DATR(1)=SIGY
        DATRIZI=SIGZ
        DATR(3)=FFX
        DATR(4)=EEY
        DATR(5)=EEZ
        DATB(8)=EPZ
        DATR(10)=ETY
        DATR(11)=ETZ
DATR(12)=CB
        DATA(13)=XX
        DATR (14) = R
DATR (15) = FY
DATR (16) = FJ1
```

DATR(17)=FJ2PR DATR(18)=EP1 RETURN ENTRY STIN2
IF (NEWPLAT) 500.510

500 ALPH=CES(5.PLATE)
RETWCFS(6.PLATE)
GAM=CES(7.PLATE)
RR=CES(8.PLATE)
DWCES(9.PLATE)
RALPH=RR\*ALPH
RGAM=RR\*GAM
CB=0.1
XX=-0.02\*ALPH
XRA=XX+RALPH
CALL COMPC(CB.XRA.RGAM.BET)
DATA(12)=CB
DATA(13)=XX
B=(CA-XX)/RR
DATA(14)=B
RETURN
510 DATA(12)=CB
DATA(13)=XX
DATA(14)=B
RETURN
SID DATA(14)=B
RETURN
END

SUBROUTINE COMPC(C.C1.C2.C3

SUBROUTINE COMPC(C.C1.C2.C3)

C NEWTONS METHOD

C COLD=C
NC=0

10 A1=C2\*EXP(C3\*C)
A2=C1-A1-C
A3=C3\*A1+1.
C=C+A2/A3
IF(ABS(C3\*(COLD=C)).LT.0.00001)GO TO 30
NC=NC+1
IF(NC.GT.20)GO TO 20
COLD=C
GO TO 10
20 WRITE(6.1000)C
1000 FORMAT(1H .4X.16HC NOT CONVERGING .E10.3)
STOP
30 IF(C.GT.0.0)C=0.
RETURN
END

### ABBREVIATIONS AND SYMBOLS

C	J, value at center of ellipse of cap model
[c]	constitutive matrix
Cijkl	compliance components
D	cap model parameter
E	Young's modulus
J <sub>1</sub>	first invariant of stress tensor = $\sigma_{ii}$
J <sub>1</sub> J <sub>2</sub>	second invariant of stress deviator tensor = $\frac{1}{2} (\sigma_{ij}^{\mathbf{d}} \sigma_{ij}^{\mathbf{d}})$
K	bulk modulus
P	pressure = -J <sub>1</sub> /3
R	ratio of major to minor axis of ellipse of cap model
W	cap model parameter
X	$J_1$ value at intersection of cap and $J_1$ -axis
Z	J <sub>1</sub> value at initial position of cap
b	$\sqrt{J_2'}$ value at center of ellipse of cap model
deke	total strain rate or increment
de <sub>kl</sub>	elastic strain rate or increment
$de^p_{ij}$	plastic strain rate or increment
dλ	scalar function
$e_{ij}^{}$ , $e_{ij}^{e}$ , $e_{ij}^{p}$	total, elastic, and plastic components of strain tensor
{e <sup>e</sup> }	elastic strain vector
f <sub>1</sub> , f <sub>2</sub>	yield functions
t	time
α, β, γ	cap model parameters which define ideal yield surface
$\delta_{ij}$	Kronecker delta
$\epsilon^{p}$	volumetric plastic strain
μ, μ <sup>e</sup> , μ <sup>p</sup>	total, elastic, and plastic volumetric compression
ν	Poisson's ratio
ρ	mass density
oij	stress components
oij oij	deviator stress components
<b>{σ}</b>	stress vector
Ψ	plastic potential function

#### REFERENCES

- Nelson, I., Baron, M. L., and Sandler, I., "Mathematical Models for Geological Materials for Wave-Propagation Studies," Shock Waves and the Mechanical Properties of Solids, Syracuse University Press, Syracuse, New York, 1971.
- 2. Sandler, I., and Rubin, D., A Modular Subroutine for the Cap Model, Report DNA 3875F, Defense Nuclear Agency, Washington, D.C., January 1976.
- 3. Sandler, I. S., DiMaggio, F. L., and Baladi, G. Y., "Generalized Cap Model for Geologic Materials," *Journal of the Geotechnical Engineering Division*, ASCE, Vol. 102, No. GT7, July 1976, pp. 683-699.
- 4. Drucker, D. C., "On Uniqueness in the Theory of Plasticity," Quar. Appl. Math., 14, 1956, pp. 35-42.
- 5. DiMaggio, F. L., and Sandler, I. S., "Material Model for Granular Soils," Journal of the Engineering Mechanics Division, Proceedings of the American Society of Civil Engineers, Vol. 97, No. EM3, June 1971, pp. 935-949.
- 6. Lawrence, R. J., and Mason, D. S., WONDY IV A Computer Program for One-Dimensional Wave Propagation with Rezoning, SC-RR-71-0284, Sandia Laboratories, Albuquerque, New Mexico, August 1971.
- 7. Zelasko, J. S., and Ingram, J. K., Soil Property Investigation and Free-Field Ground Motion Measurements, Project BACKFILL, USAEWES, Vicksburg, Mississippi, December 1967.
- 8. Mazanti, B. B., and Holland, C. N., Study of Soil Behavior Under High Pressure, Report 1: Response of Two Recompacted Soils to Various States of Stress, Report S-70-2, USAEWES, Vicksburg, Mississippi, February 1970.
- 9. Bratton, J. L., Fedock, J., and Higgins, C. J., A Parametric Study of the Effects of Material Properties Upon Cylindrical Wave Propagation, AFWL Technical Note (in preparation).
- 10. Isenberg, J., Collins, J. D., and Kennedy, B., Statistical Estimations of Geological Material Model Parameters from Cylindrical In-Situ Test Data, AFWL-TR-76-187, Air Force Weapons Laboratory, Kirtland Air Force Base, New Mexico.
- 11. Isenberg, J., Automated Data Analysis Application of Statistical Estimation of Geological Material Model Parameters, AFWL Technical Report (in preparation).

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1	Terra Tek, Inc., 420 Wakara Way, Salt Lake City, UT 84108 Dr. H. R. Pratt
1 1	TRW Systems Group, San Bernardino Operations, P.O. Box 1310 San Bernardino, CA 92402 Mr. Bing Fay Mr. Greg Hulcher
1 1 1	TRW Systems Group, One Space Park, Redondo Beach, CA 90278 Mr. Norm Lipner Dr. Peter K Dai, R1/2178 Dr. Benjamin Sussholtz
1 1 1	University of Illinois, 133 Davenport House, 807 South Wright St., Champaign, IL 61820 Dr. Nathan M. Newmark Dr. Skip Hendron Dr. Bill Hall
1	University of Oklahoma, Dept. of Info. & Computing Science, 905 Asp, Norman, OK 73069 Dr. John Thompson
1 1 1	University of New Mexico, Civil Engineering Research Facility, Albuquerque, NM 87106 Mr. Del Calhoun Mr. D. J. Higgins Mr. Joe Fedock
1	University of Texas, Dept. of Geological Sciences, Austin, TX 78712 Mr. William R. Muehlberger
1	Virginia Polytechnic Institute, Dept. of Civil Engineering, Blacksburg, VA 24061 Dr. C. S. Desai
1	Weidlinger, Paul, Consulting Engineer, 110 East 59th Street, New York, NY 10022 Dr. Melvin L. Baron
1	Weidlinger Associates, 2710 Sand Hill Road., Menlo Park, CA 94025 Dr. J. Isenberg

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J. H. Wiggins Co., 1650 Pacific Coast Hwy., Redondo Beach, CA 90277 Dr. Jon Collins

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